

Lesson 18: Inference for Two Proportions

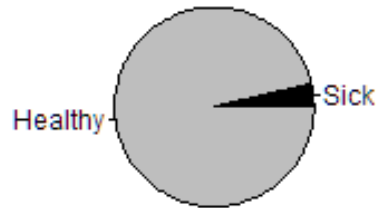
Homework

Solutions

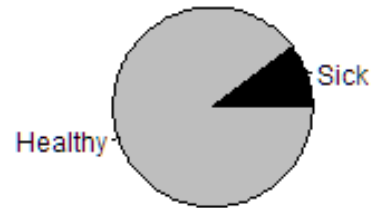
Please note that the steps show rounded numbers, but that the final answers to the problems are calculated without rounding.

Problem	Part	Solution
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Rural Communities



Urban Communities



1 -

2 -

$$n_1 \times \hat{p}_1 \geq 10 \text{ and } n_1 \times (1 - \hat{p}_1) \geq 10$$

$$261 \times (0.038) = 10 \geq 10 \text{ and } 261 \times (1 - 0.038) = 251 \geq 10$$

$$n_2 \times \hat{p}_2 \geq 10 \text{ and } n_2 \times (1 - \hat{p}_2) \geq 10$$

$$1614 \times (0.103) = 166 \geq 10 \text{ and } 1614 \times (1 - 0.103) = 1448 \geq 10$$

3 -

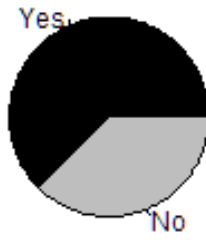
The requirements are met.
 (-0.092 , -0.037) We are 95 % confident that the true difference of the proportions of city children with hay fever and rural children with hay fever is between -0.092 and -0.037 .

4 -

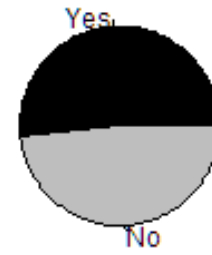
If you swapped the definition of groups 1 and 2, then you would get the same values with opposite signs: (0.037 , 0.092). This is also correct.
 No. This means that it is plausible that the likelihood of a child contracting hay fever is different in the city than in rural areas.

Problem	Part	Solution
5	-	$n_1 \times \hat{p}_1 \geq 10$ and $n_1 \times (1 - \hat{p}_1) \geq 10$ $200,000 \times (0.0002) = 33 \geq 10$ and $200,000 \times (1 - 0.0002) = 199,967 \geq 10$ $n_2 \times \hat{p}_2 \geq 10$ and $n_2 \times (1 - \hat{p}_2) \geq 10$ $200,000 \times (0.0006) = 115 \geq 10$ and $200,000 \times (1 - 0.0006) = 199,885 \geq 10$
6	-	<p>The requirements are met. (-0.00053 , -0.00029) We are 95 % confident that the true difference of the proportions of vaccinated children who developed polio and non-vaccinated children who developed polio is -0.00053 and -0.00029 .</p> <p>If you swapped the definition of groups 1 and 2, then you would get the same values with opposite signs: (0.00029 , 0.00053). This is also correct.</p>

Male Cheaters

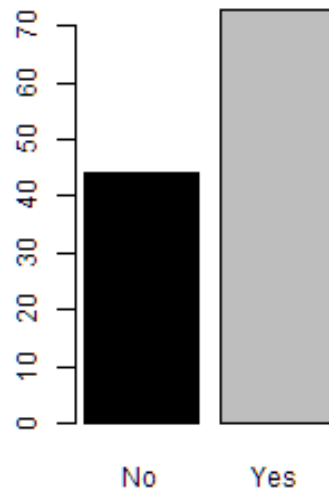


Femal Cheaters

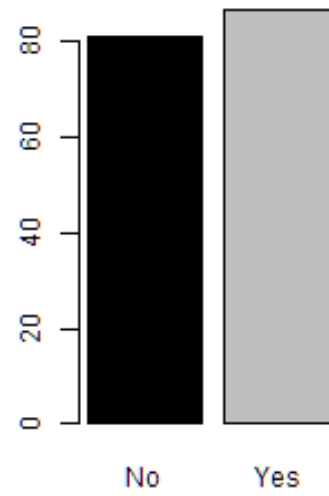


7 -

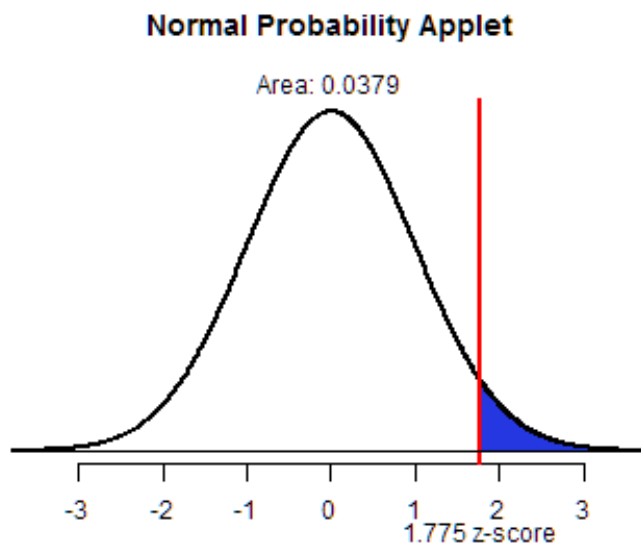
Male Cheaters



Female Cheaters



Problem	Part	Solution
8	-	$n_1 \times \hat{p}_1 \geq 10$ and $n_1 \times (1 - \hat{p}_1) \geq 10$ $117 \times (0.624) = 73 \geq 10$ and $117 \times (1 - 0.624) = 44 \geq 10$ $n_2 \times \hat{p}_2 \geq 10$ and $n_2 \times (1 - \hat{p}_2) \geq 10$ $168 \times (0.518) = 87 \geq 10$ and $168 \times (1 - 0.518) = 81 \geq 10$ The requirements are met.
9	-	$H_0 : p_1 = p_2$ $H_a : p_1 > p_2$
10	-	$\hat{p}_1 = 0.624$ $\hat{p}_2 = 0.518$
11	-	$z = 1.775$
12	-	p-value = 0.038



- 13 -
- 14 - reject the null hypothesis
- 15 - There is sufficient evidence to suggest that the proportion of men who cheat in college is greater than the proportion of women who cheat in college.
- 16 - The p-value would double and be equal to 0.076 . This p-value is not significant and we would fail to reject the null hypothesis. With a two sided test we would not have sufficient evidence to conclude that there is a difference between the proportion of women and men who cheat in college.

